

1. The expression $ab + 3c - 3b - ac$ is equal to

- (A) $(a - 3)(b - c)$
- (B) $(a + 3)(b - c)$
- (C) $(a - 3)(b + c)$
- (D) $(a + 3)(c - b)$

2. The linear factor of $x^3 - 3x^2 - 3x - 4$ is

- (A) $x - 1$
- (B) $x - 2$
- (C) $x + 2$
- (D) $x - 4$

3. Given that $f(x) = 6 - x - 2x^2$ is less than or equal to k , where $k \in \mathbb{R}$, then k is equal to

- (A) $-\frac{49}{8}$
- (B) $-\frac{1}{4}$
- (C) $\frac{1}{4}$
- (D) $\frac{49}{8}$

4. Given that $f(x) = 1 - 4x - 2x^2$, then $f(x)$ can be expressed in the form

- (A) $2(x + 1)^2 - 3$
- (B) $3 - 2(x - 1)^2$
- (C) $3 - 2(x + 1)^2$
- (D) $3 - (2x + 1)^2$

5. A quadratic equation is such that the sum of its roots is $-\frac{2}{3}$ and the product of its roots is $\frac{3}{4}$. The quadratic equation is

- (A) $12x^2 + 8x + 9 = 0$
- (B) $12x^2 - 8x - 9 = 0$
- (C) $12x^2 - 8x + 9 = 0$
- (D) $12x^2 + 8x - 9 = 0$

6. Given that $x > 0$, the set of values of x for which $x - 2 < \frac{15}{x}$ is

- (A) $\{x: x > 0 \cup x > 5\}$
- (B) $\{x: 0 < x < 5\}$
- (C) $\{x: x > 5\}$
- (D) $\{x: x < 5\}$

7. Given that $f(x) = 13x - 6 - 2x^2$, the values of x for which $f(x) < 0$ are

- (A) $x > \frac{1}{2}$ and $x > 6$
- (B) $x < \frac{1}{2}$ and $x > 6$
- (C) $x < -\frac{1}{2}$ and $x > 6$
- (D) $x > \frac{1}{2}$ and $x < 6$

8. If $f(x) = \frac{1}{8}x^3$, $x \in \mathbb{R}$ and $-2 \leq x \leq 4$, then

- (A) $-8 \leq f(x) \leq 64$
- (B) $8 \leq f(x) \leq 64$
- (C) $-1 \leq f(x) \leq 8$
- (D) $-2 \leq f(x) \leq 4$

9. If $f: x \rightarrow 2\left(\frac{x}{3} + 5\right)$, then $f^{-1}(x)$ is equal to

(A) $3\left(\frac{x}{2} - 5\right)$

(B) $3\left(\frac{x}{2} + 5\right)$

(C) $\frac{1}{3}\left(\frac{x}{2} - 5\right)$

(D) $\frac{3(x-2)}{5}$

10. If $f(x) = \frac{x+1}{x-2}$, $x \neq 2$, $x \in \mathbb{R}$,

then $ff(x) =$

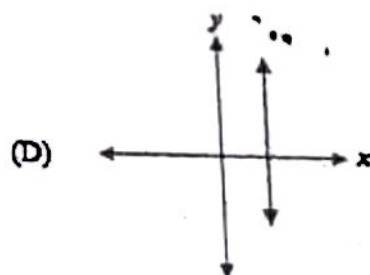
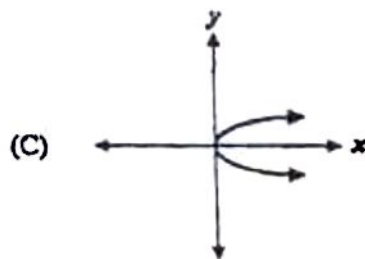
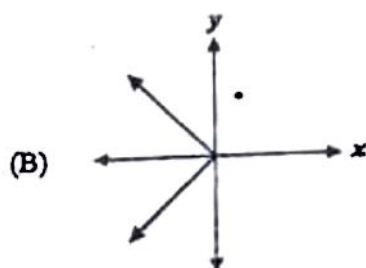
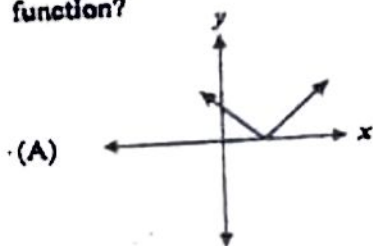
(A) $\frac{2x-1}{-3-x}$, $x \neq -3$, $x \in \mathbb{R}$

(B) $\frac{2x-1}{5-x}$, $x \neq 5$, $x \in \mathbb{R}$

(C) $\left(\frac{x+2}{x-2}\right)^2$, $x \neq 2$, $x \in \mathbb{R}$

(D) $\frac{2x-1}{3x+5}$, $x \neq -\frac{5}{3}$, $x \in \mathbb{R}$

11. Which of the following graphs depicts a function?



12. $\sqrt[3]{3 \times 27^n}$ is equal to
- (A) $3^{\frac{4n}{3}}$
 (B) 3^{n+3n}
 (C) $\sqrt[3]{81^{3n}}$
 (D) $3^{\frac{3n+1}{n}}$
13. The value of x for which $9^{2x} = 3$ is
- (A) $-\frac{3}{2}$
 (B) $-\frac{1}{2}$
 (C) $\frac{3}{2}$
 (D) $\frac{5}{2}$
14. Given that $\log_2 x^3 = 6$, then the value of x is
- (A) 2
 (B) 4
 (C) 8
 (D) 64
15. The value of $\sqrt{18} + \sqrt{50}$ is
- (A) $34\sqrt{2}$
 (B) $6\sqrt{15}$
 (C) $8\sqrt{2}$
 (D) $\sqrt{68}$
16. The value of x for which $3^{x+2} + 3^x = 90$ is
- (A) $\frac{1}{2} \left(\frac{\log 90}{\log 3} - 2 \right)$
 (B) 2
 (C) 44
 (D) $\left(\frac{\log 10}{\log 3} \right)$
17. The series $-2 + \frac{4}{3} - \frac{8}{9} + \dots$ converges to the limit
- (A) -6
 (B) 6
 (C) $-\frac{6}{5}$
 (D) $\frac{6}{5}$
18. What is the sum of the ODD integers between 10 and 50?
- (A) 60
 (B) 600
 (C) 630
 (D) 1960
19. The common ratio of the geometric sequence 8, 12, 18, ... is
- (A) $\frac{1}{2}$
 (B) $\frac{2}{3}$
 (C) $\frac{3}{4}$
 (D) $\frac{3}{2}$

20. A sequence of positive integers $\{U_n\}$ is defined by $U_n = 3\left(\frac{1}{2}\right)^{n-1}$. The 10th term of the sequence is given by

- (A) $\frac{19\,683}{512}$
 (B) $\frac{3}{256}$
 (C) $\frac{3}{512}$
 (D) $\frac{3}{1000}$

21. The point $(2, 3)$ is at one end of a diameter of a circle whose equation is

$$x^2 + y^2 - 10x + 2y + 1 = 0.$$

The coordinates of the other end of the diameter are

- (A) $(8, -1)$
 (B) $(8, -5)$
 (C) $(-12, -1)$
 (D) $(-12, -5)$

22. The line through the points $Q(h, 2)$ and $R(4, 8)$ is parallel to the line with equation $2x + y - 10 = 0$. The value of h is

- (A) 1
 (B) 2
 (C) -7
 (D) 7

23. The line $y = 2x - 7$ and the line $x + 3y = 7$ intersect at the point

- (A) $(4, 1)$
 (B) $(8, 6)$
 (C) $(-5, 4)$
 (D) $(0, -7)$

24. The vectors i and j represent 1 km/h east and north respectively. A man sails a boat on a lake such that the velocity is $-i + 2j$ when there is no current. If there is a current of $3i$, then the resultant velocity, v , is given by

- (A) $2i + 2j$ km/h
 (B) $4i - 2j$ km/h
 (C) $-4i + 2j$ km/h
 (D) $-4i - 2j$ km/h

25. The vector a is given as $5i + 12j$. A unit vector parallel to a is

- (A) $15i + 36j$
 (B) $195i + 468j$
 (C) $\frac{1}{13}(5i + 12j)$
 (D) $\frac{3}{13}(5i + 12j)$

26. The position vector of two points A and B relative to an origin O are given by

$$\vec{OA} = \begin{pmatrix} 3 \\ 0 \end{pmatrix} \text{ and } \vec{OB} = \begin{pmatrix} 8 \\ 5 \end{pmatrix} \text{ respectively.}$$

The modulus of \vec{AB} and the angle \vec{AB} makes with the x -axis respectively are

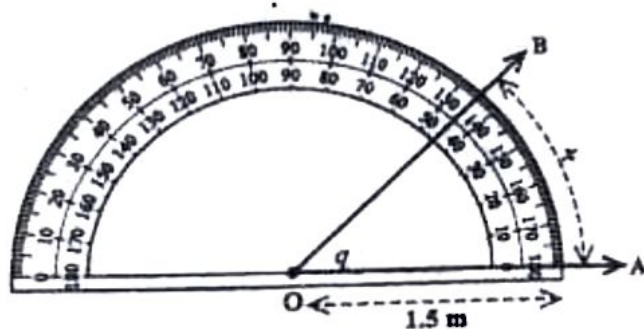
- (A) modulus = 10, angle = 45°
 (B) modulus = 10, angle = 30°
 (C) modulus = $\sqrt{50}$, angle = 45°
 (D) modulus = $\sqrt{50}$, angle = 90°

27. The trigonometrical expression

$$\frac{\sin x}{1 - \cos x} + \frac{\sin x}{1 + \cos x} \text{ is identical to}$$

- (A) $2 \sin x$
- (B) $2 \tan x$
- (C) $\tan^2 x$
- (D) $\frac{2}{\sin x}$

Item 28 refers to the following protractor which represents half of a circle. The protractor has a radius of 1.5 metres and the angle AOB measures 45° .



28. What is the arc length, x , in metres, along the outer edge of the protractor?

- (A) $\frac{\pi}{4}$
- (B) $\frac{3\pi}{8}$
- (C) $\frac{3\pi}{4}$
- (D) $\frac{\pi}{6}$

29. The graph of $y = \sin 2x$ is

- (A)

A graph showing a sine wave starting at (0,0), reaching a peak at $y=2$ when $x=\pi$, and returning to the x-axis at $x=2\pi$. The y-axis is labeled from -2 to 2.
- (B)

A graph showing a sine wave starting at (0,0), reaching a peak at $y=1$ when $x=\pi/2$, crossing the x-axis at $x=\pi$, reaching a trough at $y=-1$ when $x=3\pi/2$, and returning to the x-axis at $x=2\pi$. The y-axis is labeled from -1 to 1.
- (C)

A graph showing a sine wave starting at (0,0), completing two full cycles between $x=0$ and $x=2\pi$. The y-axis is labeled from -1 to 1.
- (D)

A graph showing a sine wave starting at (0,0), completing four full cycles between $x=0$ and $x=2\pi$. The y-axis is labeled from -1 to 1.

30. If $\sin(x + 20^\circ) = \cos x$, then the value of x is

- (A) 35°
- (B) 45°
- (C) 55°
- (D) 70°

37. $\frac{d}{dx} \left(\frac{2x-1}{5-x} \right) =$

(A) $\frac{9}{(5-x)^2}$

(B) $\frac{-9-4x}{(5-x)^2}$

(C) $-\frac{9}{(5-x)^2}$

(D) $\frac{9-4x}{(5-x)^2}$

38. Given $y = 2x^2 + 3 \cos x$, then $\frac{dy}{dx} =$

(A) $x + \sin x$

(B) $x - \sin x$

(C) $4x - 3 \sin x$

(D) $4x + 3 \sin x$

39. The curve C with equation $y = f(x)$ has a stationary point at $(-2, 5)$.

If $f''(x) = x^2 - 15$, then $(-2, 5)$ is

(A) a vertex

(B) an intercept

(C) a minimum turning point

(D) a maximum turning point

40. $\int_0^2 (3x+4)^3 dx =$

(A) 812 units²

(B) 821 units²

(C) 830 units²

(D) 854 $\frac{2}{3}$ units²

41. The solution to $\int_{-1}^1 \frac{1}{(5x-2)^2} dx$ is

(A) $\frac{1}{35} - \frac{1}{110}$

(B) $\frac{1}{35} + \frac{1}{110}$

(C) $-\frac{1}{35} - \frac{1}{110}$

(D) $-\frac{1}{35} + \frac{1}{110}$

42. $\int_1^4 (2x-4)^3 dx =$

(A) $(2x-4)^4 + k$

(B) $\frac{(2x-4)^4}{2} + k$

(C) $\frac{(2x-4)^2}{8} + k$

(D) $\frac{(2x-4)^4}{8} + k$

43. A curve C passes through the point $(2, -5)$.

The gradient of the curve at the point (x, y) is given by $\frac{dy}{dx} = 7 - x^2$. The equation of the curve is

- (A) $y = 7x - \frac{1}{4}x^4 - 15$
- (B) $y = 7x - 3x^2 - 7$
- (C) $y = -3x^2 + 7$
- (D) $y = 7 - x^2$

45. $\int (\cos x - 2 \sin x) dx =$

- (A) $-\cos x + \sin x + c$
- (B) $\cos x - 2 \sin x + c$
- (C) $\cos x - \sin x + c$
- (D) $2 \cos x + \sin x + c$

44. If $\int_1^4 f(x) dx = 6$, then $\int_1^4 4f(x) dx + 5 =$

- (A) 9
- (B) 11
- (C) 29
- (D) 44